

Determination of the "Meridian Convergence" and the "Scale Factor" at Chajnantor.

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$$\phi := -1 \cdot \left(23 + \frac{1}{60} + \frac{10}{3600} \right) \cdot \frac{\pi}{180}$$

$$\lambda := -1 \cdot \left(67 + \frac{45}{60} + \frac{10}{3600} \right) \cdot \frac{\pi}{180}$$

$$\lambda_0 := -1 \cdot 69 \cdot \frac{\pi}{180}$$

$$l := \lambda - \lambda_0 \quad \text{Longitude difference}$$

The second excentricity on the Hayford Elipsoid (reference to the PSAD-56 datum) is:

$$e_p := \sqrt{0.006768170197}$$

$$a_7 := \sin(\phi)$$

$$a_9 := \frac{1}{3} \cdot \sin(\phi) \cdot \cos(\phi)^2 \cdot \left(1 + 3 \cdot e_p^2 \cdot \cos(\phi)^2 + 2 \cdot e_p^4 \cdot \cos(\phi)^4 \right)$$

$$a_{11} := \frac{1}{15} \cdot \sin(\phi) \cdot \cos(\phi)^2 \cdot \left(-1 + 3 \cdot \cos(\phi)^2 \right)$$

Hence, the meridian convergence (in degrees) is the following

$$C := \left(a_7 \cdot l + a_9 \cdot l^3 + a_{11} \cdot l^5 \right) \cdot \frac{180}{\pi}$$

$C = -0.48778453$ Negative value indicates the grid's north is west of the geographic north

Determination of the scale factor

$$a_8 := \frac{1}{2} \cdot \cos(\phi)^2 \cdot \left(1 + e_p^2 \cdot \cos(\phi)^2 \right)$$

$$a_{10} := \frac{1}{24} \cdot \cos(\phi)^2 \cdot \left[-4 + \left(9 - 28 \cdot e_p^2 \right) \cdot \cos(\phi)^2 + 42 \cdot e_p^4 \cdot \cos(\phi)^4 \right]$$

$$m := 1 + a_8 \cdot l^2 + a_{10} \cdot l^4$$

$$m = 1.00020188$$